

**Project 1: Span**  
**Individual Assignments**  
**April 13, 2024**

Version: 445

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$$v_1 = \begin{pmatrix} 3 \\ -2 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -2 \\ -4 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} -1 \\ -10 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

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Version: 522

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$$v_1 = \begin{pmatrix} -2 \\ -3 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -2 \\ 1 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} -6 \\ -1 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -2 \\ -3 \end{pmatrix}$$

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Version: 555

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$$v_1 = \begin{pmatrix} -2 \\ -3 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -3 \\ 1 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} 1 \\ -4 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -2 \\ -1 \end{pmatrix}$$

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Version: 658

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 $v_1 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 0 \\ -5 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$   
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Version: 769

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 $v_1 = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -4 \\ -1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 5 \\ -7 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 2 \\ -2 \end{pmatrix}$   
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Version: 803

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 $v_1 = \begin{pmatrix} 4 \\ -3 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 3 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -1 \\ 4 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -1 \\ -2 \end{pmatrix}$   
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Version: 906

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 $v_1 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -2 \\ -4 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -5 \\ -6 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -4 \\ 2 \end{pmatrix}$   
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Version: 1108

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 $v_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -2 \\ 2 \end{pmatrix}$   
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Version: 1257

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 $v_1 = \begin{pmatrix} -4 \\ 2 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -5 \\ 10 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$   
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Version: 1402

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 $v_1 = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -4 \\ -2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 2 \\ 6 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -2 \\ -2 \end{pmatrix}$   
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Version: 1415

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 $v_1 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ -3 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -1 \\ 4 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -2 \\ 2 \end{pmatrix}$   
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Version: 1526

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$$v_1 = \begin{pmatrix} -4 \\ 1 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} 0 \\ 5 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -3 \\ -4 \end{pmatrix}$$

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Version: 1553

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$$v_1 = \begin{pmatrix} -3 \\ 2 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} 4 \\ 3 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} 7 \\ 1 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

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Version: 1598

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$$v_1 = \begin{pmatrix} -1 \\ -2 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} 1 \\ -3 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} -5 \\ -5 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} 8 \\ -2 \end{pmatrix}$$

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Version: 1626

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$$v_1 = \begin{pmatrix} -1 \\ 1 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -2 \\ -1 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} 4 \\ -1 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -4 \\ 3 \end{pmatrix}$$

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Version: 1708

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 $v_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 6 \\ -1 \end{pmatrix}$   
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Version: 1708

-----  
 $v_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 6 \\ -1 \end{pmatrix}$   
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Version: 1724

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 $v_1 = \begin{pmatrix} -2 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -3 \\ 3 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -4 \\ 7 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 1 \\ -3 \end{pmatrix}$   
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Version: 1724

-----  
 $v_1 = \begin{pmatrix} -2 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -3 \\ 3 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -4 \\ 7 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 1 \\ -3 \end{pmatrix}$   
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Version: 1834

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 $v_1 = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 4 \\ 4 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -7 \\ -10 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 3 \\ 1 \end{pmatrix}$   
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Version: 1989

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 $v_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -1 \\ 5 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -5 \\ -2 \end{pmatrix}$   
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Version: 2064

-----  
 $v_1 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -4 \\ 4 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -2 \\ 5 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -1 \\ -1 \end{pmatrix}$   
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Version: 2079

-----  
 $v_1 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -3 \\ 0 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 4 \\ -6 \end{pmatrix}$   
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Version: 2169

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 $v_1 = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 0 \\ 7 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$   
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Version: 2169

-----  
 $v_1 = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 0 \\ 7 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$   
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(3.) Given  $x = \begin{pmatrix} 0 \\ 7 \end{pmatrix}$ , find  $[x]_B = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$

(4.) Given  $[y]_B = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$ , find  $y = \begin{pmatrix} -3 \\ -1 \end{pmatrix}$

Version: 2211

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 $v_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 3 \\ 1 \end{pmatrix}$   
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Version: 2330

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 $v_1 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 2 \\ 10 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 4 \\ -6 \end{pmatrix}$   
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Version: 2421

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 $v_1 = \begin{pmatrix} 1 \\ -4 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -4 \\ -5 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -1 \\ 2 \end{pmatrix}$   
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(3.) Given  $x = \begin{pmatrix} -4 \\ -5 \end{pmatrix}$ , find  $[x]_B = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$

(4.) Given  $[y]_B = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$ , find  $y = \begin{pmatrix} -5 \\ 6 \end{pmatrix}$

Version: 2452

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 $v_1 = \begin{pmatrix} -2 \\ 2 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} -8 \\ -1 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 2 \\ -2 \end{pmatrix}$   
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Version: 2583

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 $v_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 0 \\ 4 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 4 \\ -4 \end{pmatrix}$   
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Version: 2602

-----  
 $v_1 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 2 \\ 6 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -6 \\ 2 \end{pmatrix}$   
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Version: 2750

-----  
 $v_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 7 \\ 5 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 7 \\ 2 \end{pmatrix}$   
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Version: 2846

-----  
 $v_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 4 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 4 \\ -6 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -2 \\ 2 \end{pmatrix}$   
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Version: 2901

$$v_1 = \begin{pmatrix} 3 \\ -1 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} 1 \\ -3 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} -10 \\ 6 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} 4 \\ -4 \end{pmatrix}$$

Version: 2915

$$v_1 = \begin{pmatrix} 3 \\ -3 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -1 \\ -3 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} 4 \\ 0 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -1 \\ 2 \end{pmatrix}$$

Version: 2993

$$v_1 = \begin{pmatrix} -3 \\ 3 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -4 \\ -3 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} -1 \\ -6 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

Version: 3057

$$v_1 = \begin{pmatrix} -2 \\ -2 \end{pmatrix} \text{ (red) and } v_2 = \begin{pmatrix} -3 \\ 2 \end{pmatrix} \text{ (blue)}$$

$$x = \begin{pmatrix} 9 \\ 4 \end{pmatrix} \text{ (position vector in Cartesian coordinates)}$$

$$\text{1st coordinate in } v_1 \text{ direction and 2nd in } v_2 \text{ direction: } \begin{pmatrix} -3 \\ 1 \end{pmatrix}$$

Version: 3087

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 $v_1 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 4 \\ 0 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} 2 \\ -5 \end{pmatrix}$   
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Version: 3115

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 $v_1 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 6 \\ -1 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -1 \\ -4 \end{pmatrix}$   
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Version: 3154

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 $v_1 = \begin{pmatrix} -2 \\ -4 \end{pmatrix}$  (red) and  $v_2 = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$  (blue)

$x = \begin{pmatrix} 1 \\ 6 \end{pmatrix}$  (position vector in Cartesian coordinates)

1st coordinate in  $v_1$  direction and 2nd in  $v_2$  direction:  $\begin{pmatrix} -1 \\ -1 \end{pmatrix}$   
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