

100	90's	80's	70's	60's	<60
0	5	4	1	7	5

Assessment 8
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Math 254

$\bar{x} = 72\%$
med = 68.28

Name: key

All truths are easy to understand once they are discovered;
the point is to discover them.

Galileo Galilei
1564 - 1642 (Italian mathematician)

No work = no credit
No CAS Calculators

Warm-ups (1 pt each):

Expand $(3-2x)^3 = 27 - 54x + 36x^2 - 8x^3$ $\infty + \infty = \underline{\infty}$ OR 16

1.) (1 pt) Please paraphrase the quote by Galileo (above). Answer using complete English sentences.

Hindsight is 20-20.

2.) (10 pts) Answer the following:

a.) How do you determine if a vector field is conservative?

check if $\text{curl } \vec{F} = 0$.

b.) What does it mean for work to be "independent of path?"

This means the work only depends on the endpoints... NOT the path between.

c.) Given an example of a conservative vector field

$f(x, y) = 2x + y$
 $\vec{\nabla} f = \langle 2, 1 \rangle \leftarrow$ conservative

d.) Give two parameterizations of $y = x^2$ on $1 \leq x \leq 3$ (make sure to include the domain of the parameter).

$x = t$ $x = e^t$
 $y = t^2$ $y = e^{2t}$
 $1 \leq t \leq 3$ $0 \leq t \leq \ln 3$

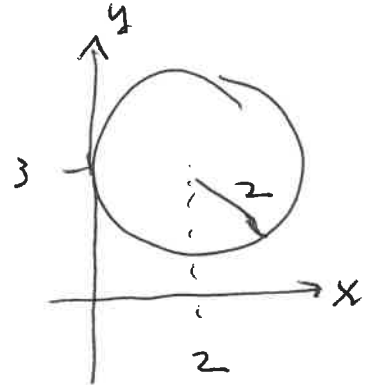
e.) Use Green's Theorem to determine what the line integral $\frac{1}{2} \oint_C -y dx + x dy$ represents geometrically.

$\frac{1}{2} \oint_C -y dx + x dy = \frac{1}{2} \iint_R 1 + 1 dA = \iint_R 1 dA$

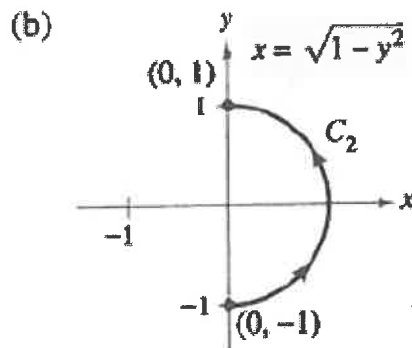
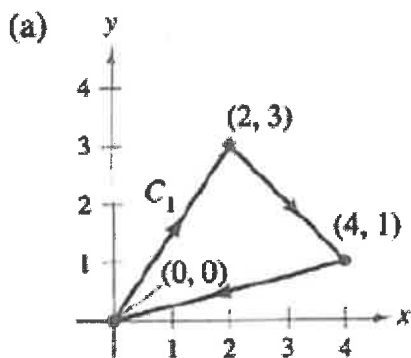
represents the area of the region enclosed by C.

work =
 3.) (10 pts) Evaluate $\oint_C (6y+x)dx + (y+2x)dy$ where C is the circle $(x-2)^2 + (y-3)^2 = 4$ traversed counter clockwise.

$$\begin{aligned} \text{work} &= \iint_R 2-6 \, dA \\ &= -4 \iint_R 1 \, dA \\ &= -4 \cdot \pi \cdot 2^2 \\ &= -16\pi \end{aligned}$$



4.) (10 pts) Consider $\int_C (2x-3y+1)dx + (5-3x-y)dy$ for the curves C_1 and C_2 .



$$\begin{aligned} f_y &= 5 - 3x - y \\ f_y &= -3x + g'(y) \\ g'(y) &= 5 - y \\ g(y) &= 5y - \frac{1}{2}y^2 + C \end{aligned}$$

$$f_x = 2x - 3y + 1$$

$$f = x^2 - 3xy + x + g(y)$$

$$f(x,y) = x^2 - 3xy + x + 5y - \frac{1}{2}y^2 + C$$

a.) Calculate $\int_{C_1} \vec{F} \cdot d\vec{r}$

$\vec{F} = \nabla f$ so \vec{F} is conservative so the work = 0.

b.) Calculate $\int_{C_2} \vec{F} \cdot d\vec{r} = f(0,1) - f(0,-1)$
 $= (5 - \frac{1}{2}) - (-5 - \frac{1}{2})$
 $= 10,$