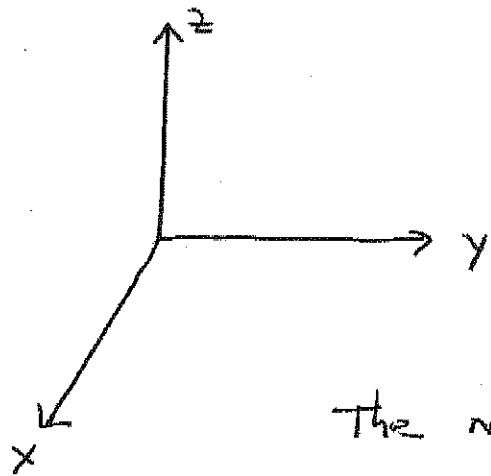


12.1
1/2

12.1: 3-D Coordinate Systems.

The axes



The right hand rule.

Locate coordinates in 3 space,

projections,

$$\mathbb{R}^3 = \{(x, y, z) \mid x, y, z \in \mathbb{R}\}$$

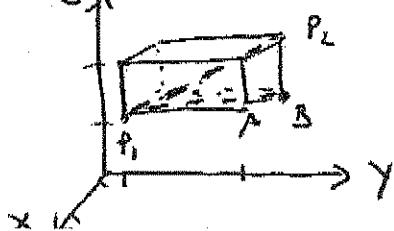
Ex 1: Plot $x=4$ and $z=-2$

Ex 2: Plot $y=x+1$ and $y=x^2+1$

Distance Formulae in \mathbb{R}^3 : The distance from

$P_1(x_1, y_1, z_1)$ to $P_2(x_2, y_2, z_2)$ is

$$|P_1 P_2| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$



$$|P_1 B|^2 = |P_1 A|^2 + |AB|^2$$

$$|P_1 P_2|^2 = |P_1 B|^2 + |BP_2|^2$$

$$= |P_1 A|^2 + |AB|^2 + |BP_2|^2$$

12.1
2/2

Ex3: Find the distance from $A(1,2,3)$
 $\rightarrow B(2,-5,8)$

Find the equation of a sphere w/ radius r
centered at (a,b,c) .

Ex4: What is $x^2 + y^2 + z^2 = 4x - 2y$ (a sphere)

Ex5: Describe $4 \leq x^2 + y^2 + z^2 \leq 25$ and $x^2 + y^2 = 1$
using a picture.

