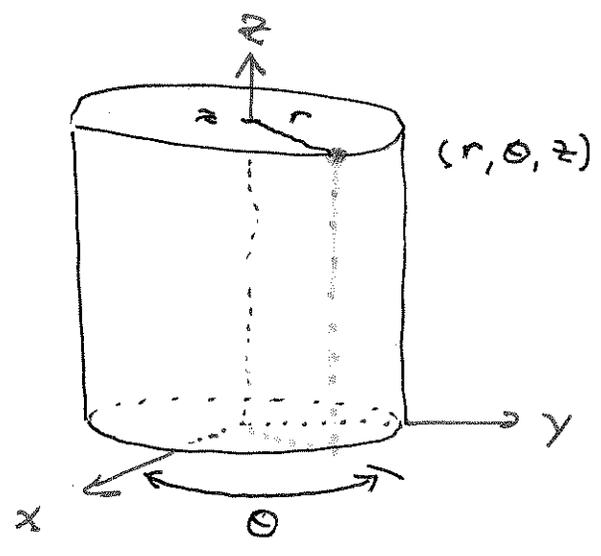


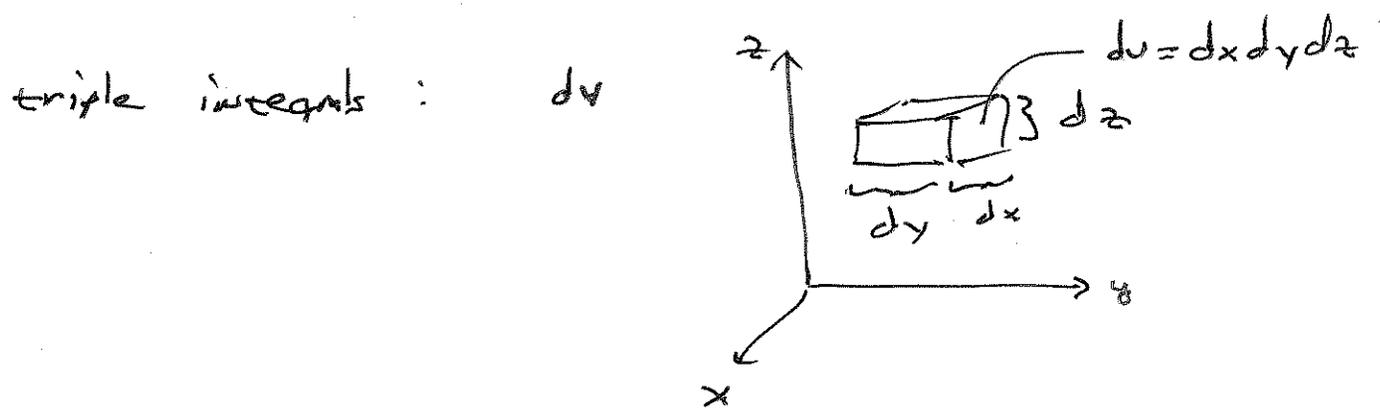
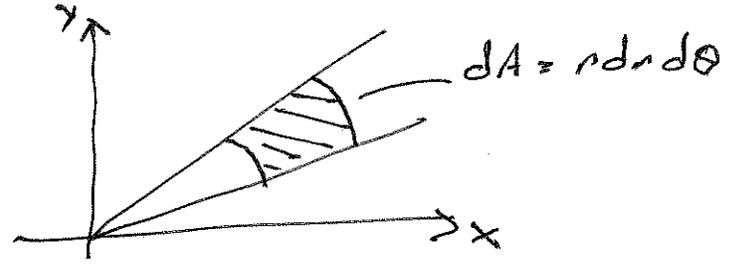
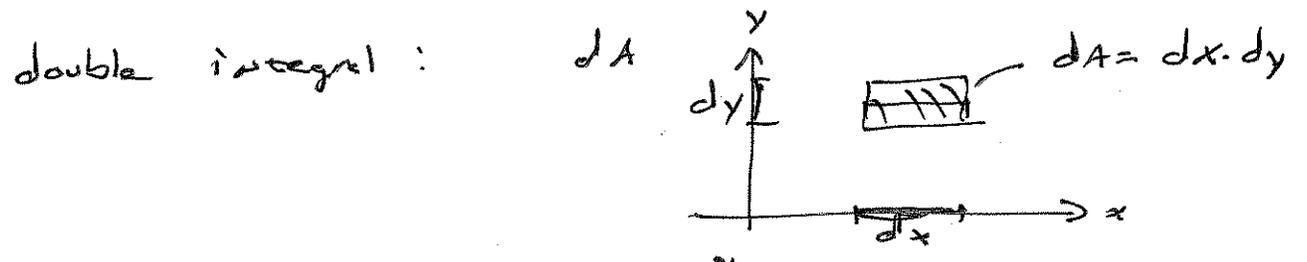
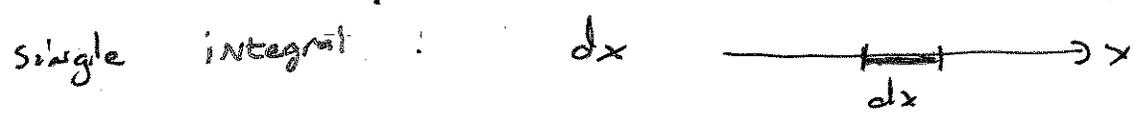
# 15.7: Triple Integrals in Cylindrical Coords

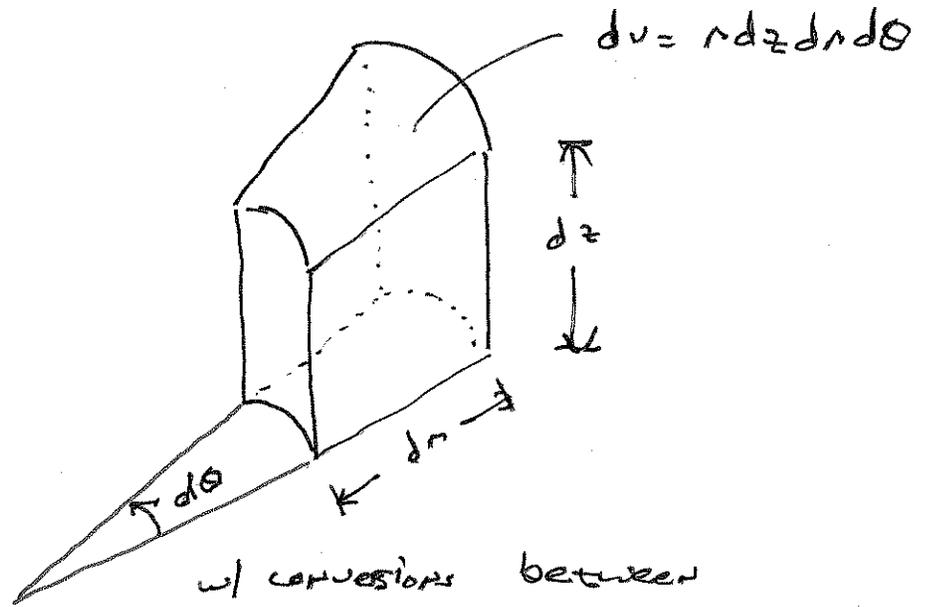
cylindrical coordinates

(sweet mathematical visualization).



## Differentials





w/ conversions between coord systems of

$$x = r \cos \theta; \quad y = r \sin \theta$$

$$x^2 + y^2 = r^2; \quad \frac{y}{x} = \tan \theta$$

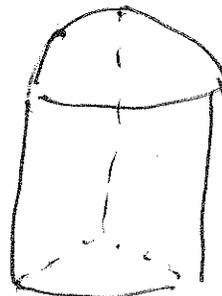
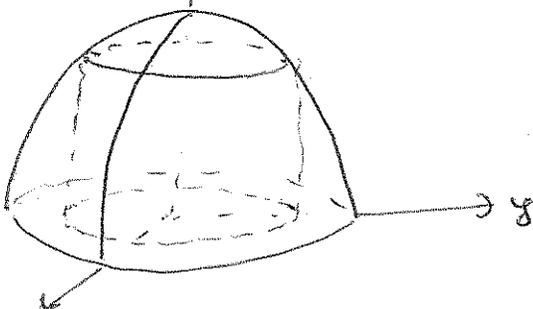
Ex 1: (A) sketch the solid whose volume is given

$$\text{by } \int_0^{\pi/2} \int_0^2 \int_0^{9-r^2} 1 \cdot r \, dz \, dr \, d\theta = 7\pi$$

(B) Express the volume using cartesian coords

(C) calculate the volume whichever way seems easier.

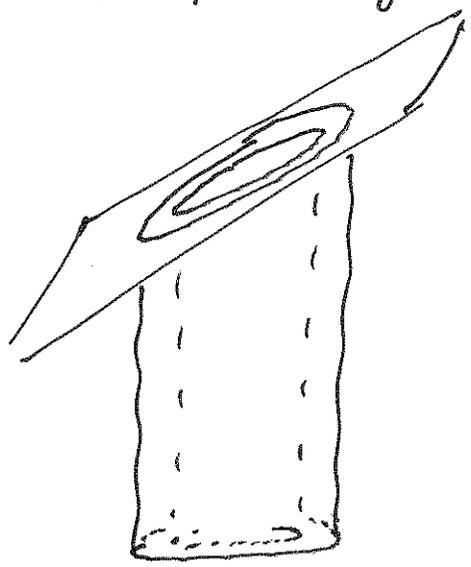
$$\int_0^2 \int_0^{\sqrt{4-x^2}} \int_0^{9-x^2-y^2} 1 \, dz \, dy \, dx = 7\pi$$



ex2: Set up an iterated integral to

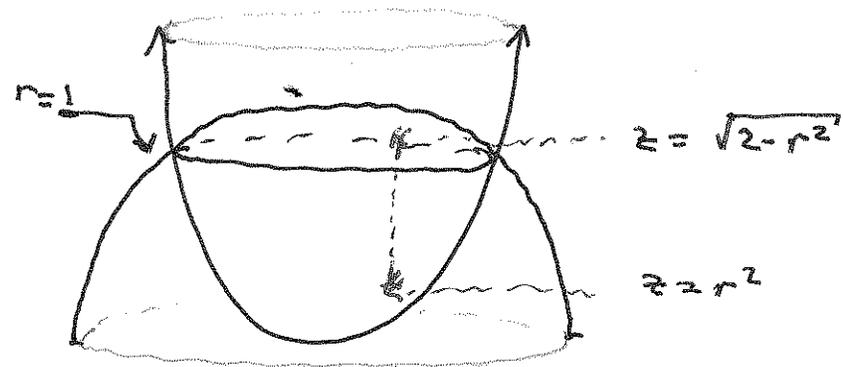
find  $I = \iiint_E x \, dV$  where  $E$  is enclosed by

$z=0$ ,  $z=x+y+5$ ,  $x^2+y^2=4$ , and  $x^2+y^2=9$



$$I = \int_0^{2\pi} \int_2^3 \int_0^{r \cos \theta + r \sin \theta + 5} r \cos \theta \cdot r \, dz \, dr \, d\theta$$

ex3: Find the volume of the solid that lies between the paraboloid  $z = x^2 + y^2$  and the sphere  $x^2 + y^2 + z^2 = 2$



Volume  $V = 4 \int_0^{\frac{\pi}{2}} \int_0^1 \int_{r^2}^{\sqrt{2-r^2}} 1 \cdot r \, dz \, dr \, d\theta$