

Test 1

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Math 111

No work = no credit

No Symbolic Calculators

Name: KEY

Why are numbers beautiful? It's like asking why is Beethoven's Ninth Symphony beautiful. If you don't see why, someone can't tell you. I know numbers are beautiful. If they aren't beautiful, nothing is.

Paul Erdos (1913 - 1996)
Hungarian mathematician

Warm-ups (1 pt each): $1+1 = \underline{2}$ $-1^2 = \underline{-1}$ $\frac{1}{0} = \underline{\text{undefined}}$

1.) (1 pt) Based upon the quote above, how did Erdos explain the beauty of numbers? Answer using complete English sentences.

It can't be explained. It must be recognized.

2.) (4 pts) Solve $\frac{3x}{4} - \frac{1}{3} = 1 - \frac{2}{3}\left(x - \frac{1}{6}\right)$

$$\Rightarrow \frac{3x}{4} - \frac{1}{3} = 1 - \frac{2}{3}x + \frac{2}{18}$$

$$\Rightarrow 27x - 12 = 36 - 24x + 4$$

$$\Rightarrow 51x = 52$$

$$\Rightarrow x = 52/51$$

3.) (4 pts) Find and interpret market equilibrium for the following supply and demand functions:

$D: p = 480 - 3q$ and $S: p = 17q + 80$.

$$480 - 3q = 17q + 80$$

$$\Rightarrow 400 = 20q$$

$$\Rightarrow q = 20$$

$$\text{and } p = 420.$$

Market equilibrium is

when 20 units are sold/bought for \$420 ea.

4.) (4 pts) Suppose a manufacturer models its monthly costs with $C(x) = 35x + 9800$ where x is in hundreds of units produced in a month and C is in dollars.

a.) Find and interpret the C -intercept.

There are fixed costs of \$9800.

b.) Find and interpret the slope.

There are variable costs of \$35/unit.

For each additional 100 units produced, costs increase \$35.

5.) (4 pts) The table gives the percent of the U.S. population that is foreign born.

a.) Find a cubic model $f(x)$ for the data where x is given in years since 1900.

$$f(x) = 0.0000571x^3 - 0.00649x^2 + 0.0446x + 14.18199$$

b.) Find and interpret $f(112)$

$$f(112) = 17.939$$

In 2012, about 17.9% of the U.S. pop is foreign born.

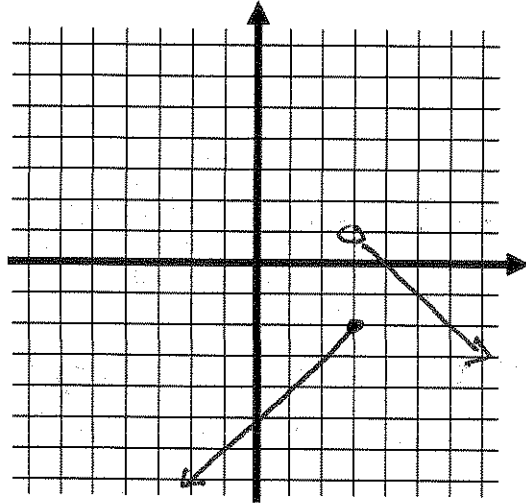
Year	% born abroad
1900	13.6
1910	14.7
1920	13.2
1930	11.6
1940	8.8
1950	6.9
1960	5.4
1970	4.7
1980	6.2
1990	8
2000	10.4
2002	11.5

6.) (4 pts) Consider $g(x) = \begin{cases} x-5, & x \leq 3 \\ 4-x, & x > 3 \end{cases}$

a.) Evaluate $g(6)$

$$g(6) = -2$$

b.) Carefully sketch a graph of $g(x)$



7.) (4 pts) Find a good viewing window for $h(x) = 0.03x - 6000$

y-inter: $(0, -6000)$

x-inter:

$$0 = 0.03x - 6000$$

$$\Rightarrow \frac{6000}{0.03} = x$$

$$[-50000, 250000] \times [-7000, 10000] \Rightarrow x = 200000$$

8.) (4 pts) Solve $5x^2 = 2x + 6$ using any method.

$$5x^2 - 2x - 6 = 0$$

$$x = \frac{2 \pm \sqrt{4 - 4(5)(-6)}}{2(5)}$$

$$= \frac{2 \pm \sqrt{124}}{10}$$

$$x \approx 1.31 \text{ OR } x \approx -0.91$$

9.) (8 pts) A certain company has fixed costs of \$15,000 for its product and variable costs given by $35 + 0.1x$ dollars per unit, where x is the total number of units. The selling price of the product is given by $285 - 0.9x$ dollars per unit.

a.) Formulate the functions for total cost, revenue, and profit.

$$C(x) = (35 + 0.1x)x + 15000 = 0.1x^2 + 35x + 15000$$

$$R(x) = (285 - 0.9x)x = -0.9x^2 + 285x$$

$$P(x) = -0.9x^2 + 285x - (0.1x^2 + 35x + 15000)$$

$$= -x^2 + 250x - 15000$$

b.) Algebraically find and interpret the break even points.

$$P(x) = -x^2 + 250x - 15000$$

$$\text{solve } 0 = -x^2 + 250x - 15000$$

$$x = \frac{-250 \pm \sqrt{250^2 - 4(-1)(-15000)}}{2(-1)}$$

$$x = 100 \text{ OR } x = 150$$

The company
breaks even when
100 OR 150 units
are produced/sold.

c.) Algebraically find and interpret the level of production and sales that maximizes profit.

$$x = 125 \text{ (mid pt.)}$$

sell 125 units to

$$x = \frac{-250}{2(-1)} = 125$$

Max profit.

$$P(125) = 625$$

d.) Find and interpret the profit (or loss) at the production level found in (c.)

The max profit is \$625.