While labeled as section 8.4, these notes are from a previous edition of the text and are equivalent to section 7.4 in the current ETV of Stewart

$$\frac{E_{x1}}{E_{x+2}} + \frac{1}{x-2} = \frac{\frac{1}{x-3} + \frac{1}{x+2}}{(x+3)(x-3)} = \frac{2x-1}{x^2-x-6}$$

$$\int \frac{2x-1}{x^2-x-6} dx = \int \left[\frac{1}{x+2} + \frac{1}{x-3}\right] dx = |w| |x+2| + |w| |x-3| + \langle |$$

$$\frac{5x2!}{x-3}$$
 $\int \frac{x^2+2x}{x-3} dx$ use poly. long div. to write
w/ deg of nom less than the
deg. of deal.

$$\frac{x+5}{x-3\sqrt{x^{2}+2x+6}}$$

$$-\frac{(x^{2}-3x)}{5x+6}$$

$$-\frac{(5x-15)}{15}$$

$$= \int \left[x + 5 + \frac{15}{x - 3} \right] dx$$

= $\frac{x^{2}}{25} + 5x + 15 \frac{10}{x - 3} + c$.

Work on your can: $\int \frac{1-x^2}{x+7} dx = \int [-x+7 - \frac{49}{x+7}] dx$ $\frac{-x+7}{-x^2+0x+1}$ $= -\frac{x^2}{2} + 7x - 48 [p] [x+7] + 6$ $\frac{-(7x+49)}{-48}$ $\underbrace{E_{X} 3}: \int \frac{X-1}{x^{2}+9_{X}+2a} dx$ $\frac{X-1}{x^{2}+9_{X}+2a} \stackrel{=}{=} \frac{X-1}{(x+5)(x+4)} \stackrel{=}{=} \frac{A}{(x+5)} \stackrel{+}{=} \frac{B}{x+4}$ product of unique
linear futers. $\Rightarrow X-1 = A(x+4) + B(x+5)$ $\Rightarrow X-1 = Ax + 4A + 6x + 5B$ $\Rightarrow \begin{cases} A + B = 1 \\ 4A + 5A = -1 \end{cases} \Rightarrow B = -5 \quad and \quad A = 6.$ $= \int \left[\frac{6}{x+5} - \frac{5}{x+4} \right] dx$

= 6 |w| + 5 | - 5 |w| + 4 + 4

8.4 3/7-

$$\frac{E_{X} + i}{x^{2} + 4x^{2} + 4x} dx = \int \frac{1 - 2x^{3}}{x(x^{3} + 4x^{2} + 4x)} dx = \int \frac{1 - 2x^{3}}{x(x + 2)^{3}} dx$$

$$paduct = \int \frac{1 - 2x^{3}}{x(x + 2)^{3}} dx$$

$$\frac{1 - 2x^{3}}{x(x + 2)^{3}} = \frac{A}{x} + \frac{B}{x + 1} + \frac{C}{(x + 2)^{3}}$$

$$\frac{1 - 2x^{3}}{x(x + 2)^{3}} = \frac{A}{x} + \frac{B}{x + 1} + \frac{C}{(x + 2)^{3}}$$

$$\frac{1 - 2x^{3}}{x(x + 2)^{3}} = A(x + 1)^{3} + Bx(x + 2) + Cx$$

$$\frac{1 - 2x^{3}}{x} = Ax^{3} + \frac{4}{x} + \frac{4}{x} + \frac{Bx^{2}}{x^{2} + 2Bx} + \frac{Cx}{x}$$

$$\frac{3}{x} \begin{cases} A + B = -2 \qquad B = -\frac{q}{4} \\ 4A + 2B + C = 0 \qquad C = \frac{3}{2}x \\ 4A + 2B + C = 0 \qquad C = \frac{3}{2}x \\ 4A - 1 \qquad A = \frac{1}{4} \end{cases}$$

$$x = \int \frac{1}{y} \frac{1}{x} - \frac{q}{4} \cdot \frac{1}{x + 2} + \frac{q}{2} \cdot \frac{1}{(x + 1)^{2}} dx$$

$$= \frac{1}{4} \frac{1}{x} \frac{1}{x} - \frac{q}{4} \frac{1}{x} \frac{1}{x + 2} + \frac{q}{2} \cdot \frac{1}{(x + 1)^{2}} dx$$

$$= \frac{1}{4} \frac{1}{x} \frac{1}{x} - \frac{q}{4} \frac{1}{x^{2} - \frac{1}{x + 2}} + \frac{q}{2} \cdot \frac{1}{(x + 1)^{2}} dx$$

$$= \frac{5x}{(x - 2)^{3}} = \frac{A}{x - 3} + \frac{D}{(x - 3)^{5}} = \int \frac{5x}{(x - 3)^{5}} dx$$

$$= \frac{5x}{(x - 2)^{3}} = \frac{A}{x - 3} + \frac{D}{(x - 3)^{5}} = \frac{1}{x - 3} + \frac{15}{4},$$

$$= \frac{5x}{x - 3} + \frac{D}{x - 3} + \frac{15}{4} = \frac{1}{x - 3} + \frac{1}{4},$$

$$= \frac{3}{x - 3} + \frac{1}{x - 3} + \frac{1}{5} = \frac{1}{5}$$

$$\frac{|Y|}{|Y|_{\frac{1}{2}}}$$

$$\frac{|X|}{|X|_{\frac{1}{2}}} = \int \frac{|X|}{|X||_{\frac{1}{2}}} dx$$

$$= \int \frac{|X|}{|X||_{\frac{1}{2}}} dx$$

$$3A = -1 \implies A = -\frac{1}{3}$$

$$= \int \left[-\frac{1}{3} \cdot \frac{1}{x} + \frac{\frac{1}{3}x+1}{x^{2}+3} \right] dx \qquad \text{for } x = x^{2}+3$$

$$= -\frac{1}{3} \ln |x| + \frac{1}{3} \int \frac{x}{x^{2}+3} dx + \int \frac{1}{x^{2}+3} dx$$

$$= -\frac{1}{3} \ln |x| + \frac{1}{3} \int \frac{x}{x^{2}+3} dx + \int \frac{1}{x^{2}+3} dx$$

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$$\frac{E_{x} 6}{\sum (x^{3} - 5x + 1)} dx = \int \frac{x^{3} - 5x + 1}{(x^{2} + 1)^{2}} dx = \int \frac{x^{3} - 5x + 1}{(x^{2} + 1)^{2}} dx = \int \frac{x^{3} - 5x + 1}{(x^{2} + 1)^{2}} dx = \int \frac{x^{3} - 5x + 1}{(x^{2} + 1)^{2}} dx = \int \frac{x^{3} - 5x + 1}{(x^{2} + 1)^{2}} dx = \int \frac{x + 5}{(x^{2} + 1)^{2}} + \frac{x + 5}{(x^{2} + 1)^{2}} = \frac{x^{2} + 5}{(x^{2} + 1)^{2}}$$

$$\frac{x^{3} - 5x + 1}{(x^{2} + 1)^{3}} = \frac{Ax + 5}{x^{2} + 2} + \frac{x + 5}{(x^{2} + 1)^{2}} + \frac{x + 5}{(x^{2} + 1)^{2}}$$

$$\frac{x^{3} - 5x + 1}{(x^{2} + 1)^{3}} = Ax^{3} + 2Ax + 5x^{2} + 25 + 6x + 0.$$

$$\frac{x^{3}}{2} = \int \frac{1}{2} + \frac{3}{2} + 2x + 5x^{2} + 2x + 6x + 0.$$

$$\frac{x^{3}}{2} = \int \frac{1}{2} + \frac{3}{2} + 2x + 5x^{2} + 2x + 5x^{2} + 2x^{2} + 5x^{2} + 5$$

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Group Work 1, Section 8.4 Partial Fractions (Version 3)

from Teaching supplementes.

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1. Compute the following integrals:

(a)
$$\int \frac{dx}{x+1}$$

(b)
$$\int \frac{dx}{x+2}$$

(c)
$$\int \frac{dx}{x^2+4}$$

2. Factor
$$x^4 + 3x^3 + 6x^2 + 12x + 8$$
. (Hint: See above)

3. Compute
$$\int \frac{20x^2 dx}{x^4 + 3x^3 + 6x^2 + 12x + 8}.$$

4. Compute
$$\int \frac{x^4 + 3x^3 + 26x^2 + 12x + 8}{x^4 + 3x^3 + 6x^2 + 12x + 8} dx$$
. (Hint: what is the degree of the purposes to devolve to ?).